

III B. TECH I SEMESTER REGULAR EXAMINATIONS, FEB-2022
DESIGN AND ANALYSIS OF ALGORITHMS
(Common to CSE and INF)

Time: 3 Hours

Max. Marks: 60

Note: Answer ONE question from each unit ($5 \times 12 = 60$ Marks)

UNIT-I

1. a) Explain the various asymptotic notations used in algorithm design? [6M]
- b) Write an algorithm to compute the n^{th} Fibonacci number? Provide time complexity analysis using step count method. [6M]

(OR)

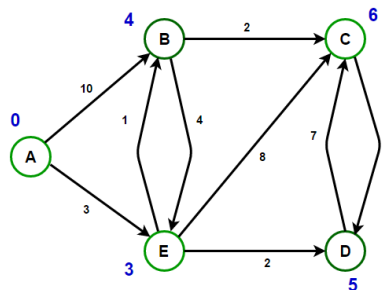
2. a) Describe divide and conquer based binary search technique with an example. [6M]
- b) Discuss the working strategy of quick sort and illustrate the process of quick sort algorithm for the given data: 43, 32, 22, 78, 63, 57, 91 and 13. [6M]

UNIT-II

3. a) Describe Knapsack problem statement? Find all feasible solutions for the following: instance of the knapsack problem: $n = 3$, $m = 20$, $(p_1, p_2, p_3) = (25, 24, 15)$, and $(w_1, w_2, w_3) = (18, 15, 10)$. [6M]
- b) Discuss Greedy algorithm to find optimal storage on tapes problem statement? Find an optimal placement for 13 programs on three tapes T_1, T_2, T_3 , where the programs are of lengths 12, 5, 8, 32, 7, 5, 18, 26, 4, 3, 11, 10, and 6. [6M]

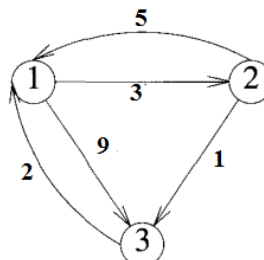
(OR)

4. a) Write greedy algorithm to find the shortest paths. [6M]
- b) Find shortest path in the following graph. [6M]



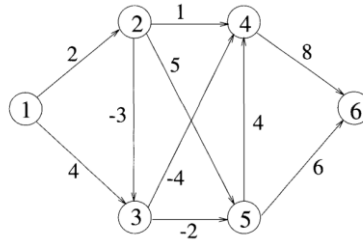
UNIT-III

5. a) What is meant by principle of optimality? Identify solution to an optimal solution to the knapsack instance $n = 5$, $M = 15$, $(p_1, p_2, \dots, p_5) = (10, 5, 15, 7, 6)$ and $(w_1, w_2, \dots, w_5) = (2, 3, 5, 7, 1)$ using dynamic programming? [6M]
- b) Illustrate all pair shortest path algorithm to find the length of shortest paths in with the following graph [6M]



(OR)

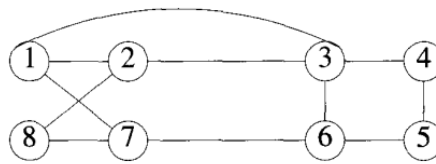
6. a) Illustrate Bellman and Ford algorithm to compute shortest paths in the following graph. [6M]



- b) Describe string editing problem? Find a minimum-cost edit sequence that transforms X into Y, Let X = a, a, b, a, a, b and Y = b, a, b, a, a. [6M]

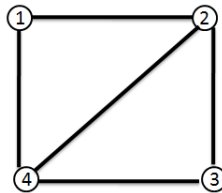
UNIT-IV

7. a) Discuss sum of subsets problem? Write recursive backtracking algorithm for sum of subsets of problem? [6M]
 b) Explain Hamilton cycle. Draw the state space generated to identify Hamilton cycles in the following graph? [6M]



(OR)

8. a) Let $w = \{5, 7, 10, 12, 15, 18, 20\}$ and $m = 35$. Find all possible subsets of w that sum to m . Draw the portion of the state space tree that is generated? [6M]
 b) Draw the state space tree for the following instance of graph coloring problem. Where $n = 4$, colors $k = 3$. [6M]



UNIT-V

9. a) Write an algorithm for a FIFO branch-and-bound search. [6M]
 b) Define branch and bound problem. Solve the following instance of Knapsack problem by Branch and bound Algorithm. $W = 15$. [6M]

Item	Weight	Profit
1	5	40
2	7	35
3	2	18
4	4	4
5	5	10
6	1	2

(OR)

10. a) Draw the portion of the state space tree generated by LCBB for the following knapsack instances: $n = 5$, $\{p_1, p_2, p_3, p_4, p_5\} = (10, 15, 6, 8, 4)$, $(w_1, w_2, w_3, w_4, w_5) = (4, 6, 3, 4, 2)$, and $m = 12$ [6M]
 b) Define the following [6M]
 (i) NP (ii) NP-competete (iii) NP-hard (iv) Cook's Theorem
